## CANADIAN BOARD OF EXAMINERS FOR PROFESSIONAL SURVEYORS

C7 - REMOTE SENSING \& PHOTOGRAMMETRY
March 2023

Although programmable calculators may be used, candidates must show all formulae used, the substitution of values into them, and any intermediate values to 2 more significant figures than warranted for the answer. Otherwise, full marks may not be awarded even though the answer is numerically correct.

Note: This examination consists of $\mathbf{1 0}$ questions on 2 pages.

## Marks

Q. No

Time: 3 hours
Value Earned


| 3. | What is the rotation matrix that relates the coordinate systems, which share the same origin, in the figure below - given that $r_{o_{2} a}^{x_{1} y_{1} x_{1}}=\left[\begin{array}{lll}-6 & 8 & 10\end{array}\right]^{T}$ and $r_{o_{2} b}^{x_{1} y_{1} x_{1}}=$ $\left[\begin{array}{ccc}6 & -8 & 10\end{array}\right]^{T}$ ? Explain conceptually and numerically how you derived such a rotation matrix. <br> Note: <br> - $r_{o_{2} a}^{x_{1} y_{1} z_{1}}$ denotes the components of the vector $o_{2} a$ w.r.t. the $x_{1} y_{1} z_{1}$ coordinate system <br> - $r_{o_{2} b}^{x_{1} y_{1} z_{1}}$ denotes the components of the vector $o_{2} b$ w.r.t. the $x_{1} y_{1} x_{1}$ coordinate system | 10 |  |
| :---: | :---: | :---: | :---: |
| 4. | What is the minimum number and optimal configuration of Ground Control Points that are needed for (justify your answer) : <br> - Dependent relative orientation of a stereo-pair, <br> - Independent relative orientation of a stereo-pair, <br> - Single photo resection, <br> - Indirect geo-referencing of an image stereo-pair, and <br> - Indirect geo-referencing of an image block with $60 \%$ overlap and $60 \%$ side lap? | 8 |  |
| 5. | a) Explain how you can use the spectral reflectance curve to identify the moisture content in vegetation and soil. <br> b) One can argue that digital cameras can see through shadow. Do you agree with this statement? Why? <br> c) What is the dynamic range of a color (RGB) digital camera that has 21 bits/pixel? <br> d) What are the parameters that are solved for (you should explain what these parameters represent) in the following photogrammetric problems: 1) Single photo resection; 2) Photogrammetric intersection; 3) Bundle adjustment; 4) Bundle adjustment with self-calibration; 5) Dependent relative orientation for a stereo-pair; and 6) Independent relative orientation for a stereo-pair)? | 2 2 2 6 |  |

\begin{tabular}{|c|c|c|c|}
\hline 6. \& \begin{tabular}{l}
a) Starting from the Collinearity equations derive the mathematical model associated with vertical photography. In other words, starting from the equations below for a general image:
\[
\begin{aligned}
\& x_{a}=x_{p}-c \frac{r_{11}\left(X_{A}-X_{o}\right)+r_{21}\left(Y_{A}-Y_{o}\right)+r_{31}\left(Z_{A}-Z_{o}\right)}{r_{13}\left(X_{A}-X_{o}\right)+r_{23}\left(Y_{A}-Y_{o}\right)+r_{33}\left(Z_{A}-Z_{o}\right)}+\text { distortion }_{x_{a}} \\
\& y_{a}=y_{p}-c \frac{r_{12}\left(X_{A}-X_{o}\right)+r_{22}\left(Y_{A}-Y_{o}\right)+r_{32}\left(Z_{A}-Z_{o}\right)}{r_{13}\left(X_{A}-X_{o}\right)+r_{23}\left(Y_{A}-Y_{o}\right)+r_{33}\left(Z_{A}-Z_{o}\right)}+\text { distortion }_{y_{a}}
\end{aligned}
\] \\
Derive the equations below for vertical photography (In your derivation, clearly state the assumptions you are making) :
\[
x_{a}=c * \frac{X_{A}}{H-h_{A}} \text { and } y_{a}=c * \frac{Y_{A}}{H-h_{A}}
\] \\
b) The overlap percentage between successive images along a given flight line does not change. Do you agree with this statement? Why? \\
c) One needs a minimum of four GNSS satellites for single point positioning using pseudo ranges. Do you agree with this statement? Why?
\end{tabular} \& \begin{tabular}{|c}
8 \\
\\
\\
\\
\\
2 \\
2
\end{tabular} \& \\
\hline 7. \& \begin{tabular}{l}
a) Height estimation using relief displacement measurements of objects closer to the nadir point is more precise than those that are farther. Do you agree with this statement? Why? \\
b) How many collinearity equations can be established for an object point that has been observed in seven images? What is the redundancy when estimating the ground coordinates of the object point - state any assumptions made in this calculation? \\
c) What are the main characteristics/differences between supervised and unsupervised classification strategies? Tabulate your answer. \\
d) Image residuals from a bundle adjustment procedure are always very small. Do you agree with this statement? Why?
\end{tabular} \& 2
3

3
2 \& <br>

\hline 8. \& | a) What are the image formation principles used for deriving the lens equation ( $1 /$ image distance +1 /object distance $=1 /$ focal length $)$ ? |
| :--- |
| b) How far is the principal point from the nadir point for a vertical image? Why? |
| c) List three advantages of increasing the overlap/side lap in an image block. |
| d) List three reasons for GNSS/INS integration for direct geo-referencing of an imaging system. | \& 2

1
3
3 \& <br>

\hline 9. \& | a) How is the perspective center defined for the lens assembly of a digital camera system? |
| :--- |
| b) The light ray from an object point to its corresponding image point is a straight line. Do you agree with this statement? Why? |
| c) What is the objective of establishing the interior orientation for a given camera? List the interior orientation parameters that we usually solve for. What are the alternative methodologies for deriving the interior orientation parameters of a photogrammetric camera? Which one would you prefer to adopt? Why? |
| d) What is the objective of establishing the exterior orientation for a given image? List the exterior orientation parameters that we usually solve for. What are the alternative methodologies for deriving the exterior orientation parameters of an imaging system? Which one would you prefer to adopt? Why? | \& 2

2
4

4 \& <br>

\hline 10. \& | a) A GPS receiver is better than a GNSS receiver. Do you agree with this statement? Why? |
| :--- |
| b) What is meant by x-parallax and y-parallax in stereo-images? |
| c) Could the following matrix be considered a rotation matrix? Why? $\left[\begin{array}{ccc} 0.7071 & 0.7071 & 0 \\ 0.7071 & -0.7071 & 0 \\ 0 & 0 & 1 \end{array}\right]$ | \& 2

2
3 \& <br>
\hline \& Total Marks: \& 100 \& <br>
\hline
\end{tabular}

