Although programmable calculators may be used, candidates must show all formulae used, the substitution of values into them, and any intermediate values to $\mathbf{2}$ more significant figures than warranted for the answer. Otherwise, full marks may not be awarded even though the answer is numerically correct.

Note: This examination consists of 9 questions on $\mathbf{3}$ pages.
Marks
O. No

Time: 3 hours
Value Earned

| 1. | Explain the difference between the following: <br> a) Precision and Accuracy <br> b) Type I and Type II errors in Statistical Testing <br> c) Internal and External Reliability <br> d) Statistically Independent and Uncorrelated | 10 |
| :---: | :---: | :---: |
| 2. | Sides $a$ and $b$ are measured once each as follows: $\begin{array}{ll} \ell & =\left[\begin{array}{l} a \\ b \end{array}\right]=\left[\begin{array}{l} 100 \\ 200 \end{array}\right] \mathrm{m} \\ C_{\ell}=\left[\begin{array}{ll} 1 & 0 \\ 0 & 4 \end{array}\right] \mathrm{cm}^{2} & C \end{array}$ <br> a) Estimate the areas of triangle ABD and the circle shown inside the rectangle. <br> b) Estimate the standard deviations of the quantities computed in Part a). <br> c) Estimate the correlation between the triangle and the circle estimates. <br> d) Discuss the nature of the correlations computed in Part c). | 15 |
| 3. | Consider that the shape of an object is defined by the following equation: $z_{i}=a x_{i}^{3}+b \sin \left(y_{i}\right)$ <br> where $z_{i}, x_{i}, y_{i}$ are observations with standard deviations $\sigma_{z_{i}}, \sigma_{x_{i}}, \sigma_{y_{i}}$, and $a$ and $b$ are parameters to be estimated. Assume $\mathrm{i}=1,2,3$. Write the linearized form of this model and derive the required matrices and vectors. | 10 |
| 4. | Given the variance-covariance matrix of the horizontal coordinates $(x, y)$ of a survey station, determine the semi-major, semi-minor axis and the orientation of the standard error ellipse associated with this station. $\mathrm{C}_{\mathrm{x}}=\left[\begin{array}{ll} 0.000532 & 0.000602 \\ 0.000602 & 0.000838 \end{array}\right] \mathrm{m}^{2}$ | 10 |




