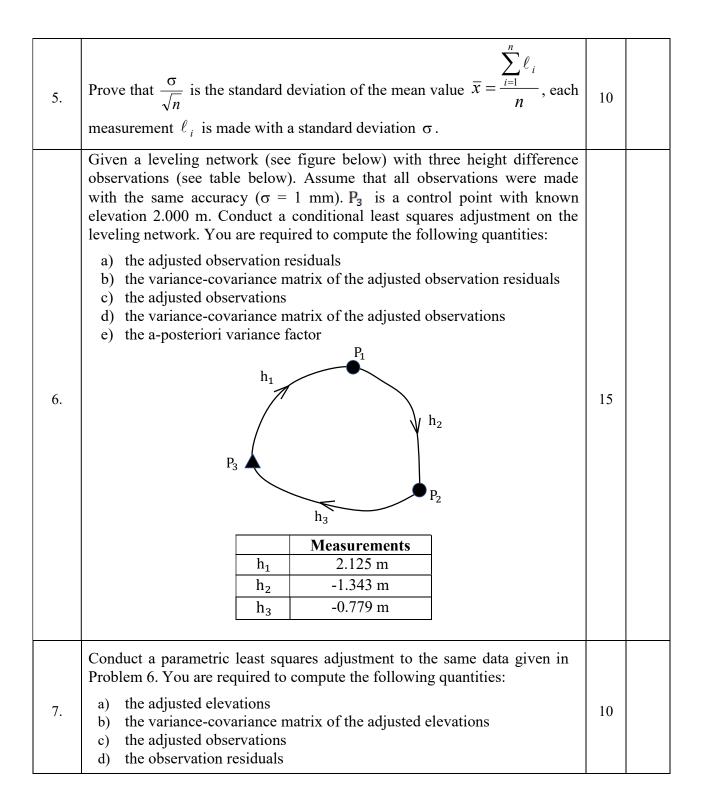
CANADIAN BOARD OF EXAMINERS FOR PROFESSIONAL SURVEYORS

C2 – LEAST SQUARES & DATA ANALYSIS

March 2022

Although programmable calculators may be used, candidates must show all formulae used, the substitution of values into them, and any intermediate values to 2 more significant figures than warranted for the answer. Otherwise, full marks may not be awarded even though the answer is numerically correct.

Note: <u>Q. No</u>	This examination consists of 9 questions on 3 pages. Time: 3 hours					
1.	Define or explain briefly the following terms: a) Accuracy b) Redundancy of a linear system c) Correlation coefficient d) External reliability e) Type II error in statistical testing	<u>Value</u> 10	Earned			
2.	Sides <i>a</i> and <i>b</i> are measured once each as follows: $I = \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} 10 \\ 20 \end{bmatrix} m$ $C_{I} = \begin{bmatrix} 1 & 0 \\ 0 & 4 \end{bmatrix} cm^{2}$ a) A A B a) Estimate the areas of triangle ABD and the circle shown inside the rectangle. b) Estimate the standard deviations of the quantities computed in Part (a). c) Estimate the correlation between the triangle and the circle estimates. d) Discuss the nature of the correlations computed in Part (c).	15				
3.	Consider that the shape of an object is defined by the following equation: $z_i = ax_i^3 + b\sin(y_i)$, $i = 1, 2, 3$. where z_i, x_i, y_i are observations with standard deviations $\sigma_{z_i}, \sigma_{x_i}, \sigma_{y_i}$, and <i>a</i> and <i>b</i> are parameters to be estimated. Derive the linearized form of this non-linear model for least squares adjustment including the required matrices and vectors.	10				
4.	Given the variance-covariance matrix of the horizontal coordinates (x, y) of a survey station, determine the semi-major, semi-minor axis and the orientation of the standard error ellipse associated with this station. $C_{x} = \begin{bmatrix} 0.000532 & 0.000602\\ 0.000602 & 0.000838 \end{bmatrix} m^{2}$	10				



8.	Given the sample network $\hat{\sigma}_0^2 = 0.5$ standard deviation adjustment result the major test step. The critical value following table: α $\chi^2_{\alpha, \nu=3}$	$5 cm^2$ with n $\sigma_0 = 0.44$ is acceptable os and explain	a degree of cm, condu e with a sig n the concl	of freedom act a statis gnificance usion.	v = 3 and $v = 3$ and $v =$	nd the a-pro- decide if = 5%. Prov	riori the vide	
	A baseline of calibrated length (μ) 200.0m is measured 5 times. Each measurement is independent and made with the same precision. The sample mean (\overline{x}) and sample standard deviation (s) are calculated from the measurements: $\overline{x} = 200.5m$ s = 0.05m Test at the 95% level of confidence if the measured distance is significantly different from the calibrated distance. The critical value that might be required in the testing is provided in the following table:							
9.	Degree of	$\begin{array}{c c c c c c c c c c c c c c c c c c c $						
	freedom	-0.90	-0.95		0.7/3	-0.99		
	1	3.08	6.31		12.7	31.8		
	2	1.89	2.92		4.30	6.96		
	3	1.64	2.35		3.18	4.54		
	4	1.53	2.13		2.78	3.75		
	5	1.48	2.01		2.57	3.36		
						Total Ma	rks: 100	