## CANADIAN BOARD OF EXAMINERS FOR PROFESSIONAL SURVEYORS ATLANTIC PROVINCES BOARD OF EXAMINERS FOR LAND SURVEYORS

## SCHEDULE I / ITEM 1 MATHEMATICS

## October 2006

**Total Marks:** 

100

## Note: This examination consists of 10 questions on 1 page. Marks <u>Q. No</u> Time: 3 hours Value Earned a. In Cartesian coordinates x and y, what is the equation of a circle of radius r with 5 1 centre at $(x_0, y_0)$ ? b. For some arbitrary point $(x_1, y_1)$ on the previous circle, what is the equation of the 5 tangent line? a. For two arbitrary vectors $\vec{\mathbf{u}}$ and $\vec{\mathbf{v}}$ , what is a formula for the angle between them? 5 2 b. How can the preceding angle formula be used to check for orthogonality and 5 parallelism of the vectors $\vec{\mathbf{u}}$ and $\vec{\mathbf{v}}$ ? a. Given a complex function $w = \sin^2 z$ for z = x + iy, what are the real and 5 3 imaginary parts of w? 5 b. What are the magnitude and argument of the preceding complex function w? a. For a small matrix A with elements $a_{11} = a_{22} = 2$ , $a_{12} = a_{21} = 1$ , what is the 5 4 determinant of A? 5 b. What are the eigenvalues of the preceding matrix A? a. For a small matrix B with elements $b_{11} = b_{22} = 2$ , $b_{12} = b_{21} = b_{13} = b_{23} = 1$ , what are 5 $BB^{T}$ and $B^{T}B$ ? 5 5 b. Which one of the preceding $BB^{T}$ and $B^{T}B$ is invertible? What is its inverse? a. Expand $(2x - 3)^{-1}$ into a power series in terms of x. Evaluate the first 3 terms only. 5 6 b. What can be said about the convergence of the corresponding series for $(2x - 3)^{-1}$ ? 5 a. Given three equations x + y + z = 5.5, x + 2y + 3z = 9.2, x + 3y + 8z = 17, what 5 7 are x, y and z by Gaussian elimination? 5 b. What are the x, y and z by applying Cramer's rule to the preceding equations? a. Given some complex transformation $w(z) = e^{z}$ , what is the corresponding inverse 5 8 complex transformation? 5 b. What are the real and imaginary parts of the preceding inverse complex function? a. For some function f(x), $d^2f(x)/dx^2 = \sin x$ , then what is the general solution f(x)? 5 9 b. For the preceding differential equation and initial conditions f(0) = 1 and df(0)/dx5 = 0, what is the solution f(x)? 5 a. For a function g(x,y), $\partial g(x,y)/\partial x = x \cos y$ , what is the general solution g(x,y)? 10 b. For the preceding partial differential equation and initial conditions g(0,0) = 1, 5

what is the solution g(x,y)?