ASSOCIATION OF CANADA LANDS SURVEYORS - BOARD OF EXAMINERS WESTERN CANADIAN BOARD OF EXAMINERS FOR LAND SURVEYORS ATLANTIC PROVINCES BOARD OF EXAMINERS FOR LAND SURVEYORS

SCHEDULE I / ITEM 1 MATHEMATICS

October 2003

| Note: | This examination consists of 10 questions on 1 page. | Marks | |
|-------------|--|--------------|--------|
| Q. No | <u>Time: 3 hours</u> | Value | Earned |
| 1.a) b) | Given two arbitrary non-parallel lines in the real plane, how can one compute the angle of intersection? Given the scalar or inner product of two unit vectors, what is the angle between them? | 5 | |
| 2.a) b) | What is the vector orthogonal to two given vectors $(1, 2, 3)^T$ and $(4, 5, 6)^T$? What is the projection of one vector $(1, 2, 3)^T$ onto another vector $(3, 5, 7)^T$? | 5 5 | |
| 3.a) b) | For an arbitrary complex variable z, what are the real and imaginary parts of the complex function $f(z) = 1 + z^2$? For an arbitrary complex variable z, what are the magnitude (or modulus) and argument (or amplitude) of the complex function $f(z) = 1 + z^2$? | 5 5 | |
| 4.a) b) | What is the polar equation of a circle of radius 2 centered at $(1,1)$? What is the polar equation of an ellipse with semi-major axis $a = 3$ and semi-minor axis $b = 2$ at the origin? | 5 5 | |
| 5.a) b) | Expand the function $y = e^{2x}$ into a power series of x at $x = 0$. Give the first three terms only. Expand the function $y = e^{x}$ into a power series of x-1 at $x = 1$. Give the first three | 5 | |
| 6.a) b) | Given a small matrix $A = [a_{ij}]$ of order 3 with elements $a_{ij} = i + j$, what is its determinant? What is the square of this matrix A? | 5 | |
| 7.a) b) | Given a small matrix $A = [a_{ij}]$ of order 2 with elements $a_{ij} = 1 + i + j$, what are its characteristic polynomial and eigenvalues or principal values? What are the corresponding eigenvectors of this matrix A? | 5 | |
| 8.a) b) | Given three equations $x + y + z = 8$, $x + 2y - z = 2$, $x - y - 3z = 4$, what are x, y and z using Cramer's rule? What are x, y and z using Gaussian elimination with these three equations? | 5 | |
| 9.a) b) | What would be a simple differential equation for $f(x) = 1 + 2x + e^x$? What is the general solution of $d^2y/dx^2 + 2y = 0$? | 5 5 | |
| 10.a) b) | What is a singular matrix? Give a matrix example of order 3. What is an hermitian matrix? Give a matrix example of order 3. | 5 5 | |
| | Total Marks: | 100 | |