

CANADIAN BOARD OF EXAMINERS FOR PROFESSIONAL SURVEYORS

C6 - GEODETIC POSITIONING

March 2012

Although programmable calculators may be used, candidates must show all formulae used, the substitution of values into them, and any intermediate values to 2 more significant figures than warranted for the answer. Otherwise, full marks may not be awarded even though the answer is numerically correct.

Note: This examination consists of 5 questions on 2 pages

Marks

<u>Q. No</u>	<u>Time: 3 hours</u>	<u>Value</u>	<u>Earned</u>
1.	<p>The ITRF96 to NAD83(CSRS) transformation parameters at epoch 1997.0 and their <u>rate of change</u> are :</p> <p>Translation and their rate of change (in meter, and meter per year respectively) $T_x = 0.9910 \text{ m}$ $T_y = -1.9072 \text{ m}$ $T_z = -0.5129 \text{ m}$ $dT_x = 0.0000 \text{ m/y}$ $dT_y = 0.0000 \text{ m/y}$ $dT_z = 0.0000 \text{ m/y}$</p> <p>Rotation and their rate of change (in milliarcsecond, and milliarcsecond per year, respectively) $R_x = -25.790 \text{ mas}$ $R_y = -9.650 \text{ mas}$ $R_z = -11.660 \text{ mas}$ $dR_x = -0.053 \text{ mas/y}$ $dR_y = 0.742 \text{ mas/y}$ $dR_z = 0.032 \text{ mas/y}$</p> <p>Scale and its rate of change $DS = 0$ $dDS = 0$ (scale and its rate of change are zero)</p> <p>a) Explain <i>with formulas</i> how this transformation (a so-called 14 parameter transformation) works.</p> <p>b) The rate of change of all parameters is zero with the exception of those related to the rotations (dR_x dR_y dR_z). Why? What do they account for?</p> <p>c) What does NAD83(CSRS) stand for? How has it been realized? What is the level of accuracy related to this datum?</p>	12	
2.	<p>Explain in details how a standalone <i>low-cost</i> GPS receiver calculates its position.</p> <ul style="list-style-type: none"> - On which observations does it rely? Which unknowns are determined? Give the observation equation (formula required). - Which additional information is needed and how does the receiver get this information? 	15	
3.	<p>a) What are the characteristics, the applications and attainable accuracy of:</p> <ul style="list-style-type: none"> - Dual-frequency Real Time Kinematic (RTK)? - Precise Point Positioning (PPP)? - Single frequency Differential GPS (DGPS)? <p>b) How does the <i>tropospheric</i> delay of the GPS signal impact the solution obtained with the above mentioned methods i.e.: RTK, PPP, DGPS?</p> <p>c) How does the <i>ionospheric</i> delay of the GPS signal impact the solution obtained with the above mentioned methods i.e.: RTK, PPP, DGPS?</p>	9 3 3	

4.	<p>Traditionally a vertical datum is established by using spirit leveling and gravity measurements.</p> <p>a) What is the reference surface used in such a vertical datum? Why does it differ from an ellipsoid and by how much with respect to an ITRF-GRS80 ellipsoid?</p> <p>b) In Canada this traditional approach will be replaced in the future by a new modern one. How will the vertical datum then be defined, realized and maintained?</p> <p>c) Nowadays GPS is widely used for positioning purposes. The height obtained from GPS is basically a height above the ellipsoid. Would it not therefore be more suitable to drop the geoid as a reference surface completely and to switch to the ellipsoid as vertical datum using ellipsoidal heights only? Argue.</p>	5	
5.	<p>The geodetic coordinates of point A and B with respect to the GRS80 ellipsoid are:</p> <p>Point-A N45° 57' 02."3453 W71°43' 21."3478 Point-B N45° 55' 54."4557 W71°43' 43."6788</p> <p>a) Calculate an approximate value for the geodetic azimuth from A to B with a resolution of 1'. (<i>just giving a numerical result without commenting on how you got it will not be accepted</i>)</p> <p>b) Explain the difference between an astronomical and a geodetic azimuth.</p> <p>c) Explain the difference between a geodetic azimuth and a grid bearing with respect to a cartographic projection.</p> <p>d) What is the maximum difference between a geodetic azimuth and a grid bearing in the UTM projection at a mid-latitude and its influence on the coordinates over a distance of 1 km?</p>	15	
		100	

Some formulae which may be helpful or not depending on the approach you opt for:

$$ds^2 = R_M^2 d\varphi^2 + R_N^2 \cos^2 \varphi d\lambda^2$$

$$R_N = \frac{a}{(1 - e^2 \sin^2 \varphi)^{1/2}} \quad \text{and} \quad R_M = \frac{a(1 - e^2)}{(1 - e^2 \sin^2 \varphi)^{3/2}}$$

GRS80-values : a = 6378137 m f = 1/298.257222101

$$(e^2 = 2f - f^2)$$