

**ASSOCIATION OF CANADA LANDS SURVEYORS - BOARD OF EXAMINERS  
WESTERN CANADIAN BOARD OF EXAMINERS FOR LAND SURVEYORS  
ATLANTIC PROVINCES BOARD OF EXAMINERS FOR LAND SURVEYORS**

**SCHEDULE I / ITEM 1  
MATHEMATICS**

**March 2006**

**Note: This examination consists of 10 questions on 1 page.**

**Marks**

**Q. No**

**Time: 3 hours**

**Value   Earned**

1	(a) Define continuity and differentiability of a function $f(x)$ on the real line. Illustrate your answer with appropriate diagrams.	5	
	(b) Give an example of a continuous function that is not differentiable at one point. Is the converse possible? Briefly explain with diagrams.	5	
2	(a) Set up the integral needed to compute the area inside a unit circle.	5	
	(b) Set up the integral needed to compute the volume inside a unit sphere.	5	
3	(a) Given a curve corresponding to $f(x,y) = 0$ in a Cartesian $(x,y)$ system, what is the normal direction at some point $(x_0, y_0)$ on the curve?	5	
	(b) Considering the same curve corresponding to $f(x,y) = 0$ in a Cartesian $(x,y)$ system, what is the curvature at $(x_0, y_0)$ on the curve?	5	
4	(a) Complex scalars have Cartesian and polar representations. What are they? How are they related? Illustrate with simple examples.	5	
	(b) Complex vectors have Cartesian and polar representations. What are they? How are they related? Illustrate with simple examples.	5	
5	(a) Given a small matrix $A = [a_{ij}]$ with elements $a_{ij} = 1 / (i + j + 2)$ , $i, j = 1, 2, 3$ , what is $A^2$ , the square of $A$ ?	5	
	(b) What is the inverse of the same matrix $A = [a_{ij}]$ with elements $a_{ij} = 1 / (i + j + 2)$ , $i, j = 1, 2, 3$ ?	5	
6	(a) Given three equations $2x + y - z = 2.25$ , $x + 3y + z = 2$ , $-x + y + 4z = 0.25$ , what are $x$ , $y$ and $z$ using Cramer's rule?	5	
	(b) What are $x$ , $y$ and $z$ using Gaussian elimination using the three equations?	5	
7	(a) Expand the exponential function $e^x$ as a power series in $x$ . Give the first five terms.	5	
	(b) Expand the exponential function $e^{\sin x}$ as a power series in $x$ . Give the first five terms only.	5	
8	(a) What is a quadratic form? How is it useful? Give a simple example.	5	
	(b) What is a Jacobian matrix in coordinate transformations? Give a simple example.	5	
9	(a) What is a singular value decomposition (SVD) of an arbitrary matrix?	5	
	(b) How is the SVD of a matrix useful in solving a system of linear equations?	5	
10	(a) What is the differential equation corresponding to a simple harmonic motion?	5	
	(b) What is the general solution for a simple harmonic motion.	5	
<b>Total Marks:</b>		<b>100</b>	